

**AT721 Homework 2**  
*Due Wed February 19*

- 1) In this problem you will run BHMIE for a single particle. You will also need the `index_water` code that calculates the index of refraction of water and ice (available in fortran and IDL). If you have a code that already does this (that you trust), and is applicable to these wavelengths, that is fine as well.
  - a. Plot the extinction efficiency, single scattering albedo and asymmetry parameter for a cloud water sphere of radius 8  $\mu\text{m}$  for wavelengths ranging from 0.4 microns to 10  $\mu\text{m}$ . Are we anywhere close to the Rayleigh regime?
  - b. Repeat part (a) in the microwave, frequency range 10 GHz to 200 GHz, for a cloud drop (radius=8 micron), drizzle drop (radius=0.1 mm) and a rain drop (radius=1 mm). For both, also calculate the Rayleigh approximation for each parameter. Where does the Rayleigh approximation roughly hold?
  - c. From the (complex) amplitude scattering matrix elements  $S_1(\Theta)$  and  $S_2(\Theta)$  for the rain drop case at a frequency of 30 GHz, plot the phase function  $P_{11}(\Theta)$  and the fractional polarization  $P_{12}(\Theta)/P_{11}(\Theta)$ . Could we consider raindrops to be strongly polarizing of radiation at this frequency, at least from a single scattering event? What might happen after multiple scattering events?
- 2) In reality we rarely run a Mie code for a single particle, but rather we typically integrate over a range of particle sizes. In this problem we'll work with a simple exponential (Marshall-Palmer type) distribution of rain drops that we will characterize in the microwave at a frequency of 30 GHz. The size distribution is written

$$N(D) = \frac{N}{D_m} \exp(-D / D_m)$$

where  $D$  is the diameter and  $N$  is the total # of drops per unit volume; it is easily shown the  $D_m$  is the mean diameter of the distribution.

- a. For a mean rain drop diameter of 3 mm, plot the drop size distribution, as well as the volume extinction coefficient per unit diameter versus diameter. Which drop size contributes the most to the extinction?
- b. Calculate the mass extinction coefficient, single scattering albedo, and asymmetry parameter of the distribution, and compare them to what you'd get if you used a single drop with either the 1) mean diameter or the 2) effective diameter. Which diameter is most closely related to the optical properties of the distribution?

*Hints:*

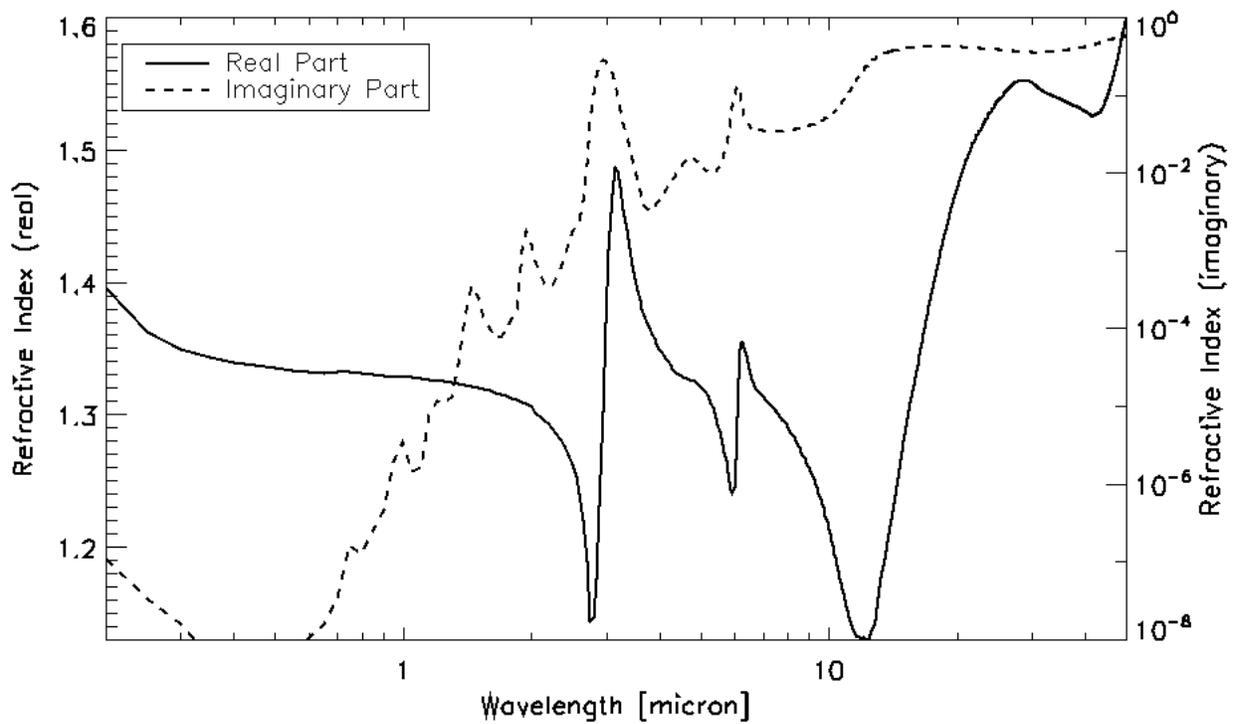
- In problem 1, it is perfect valid to attempt to use the Rayleigh approximation to calculate a single-scattering albedo (which generally will NOT equal zero).
- In problem 2, be sure to integrate far enough out in the size distribution. The quantity of primary interest is  $D^2 N(D)$ , as this is how the extinction efficiency goes per size bin.

Codes you will need:

**bhmie** (in fortran or IDL). You may also try to download a matlab or python version if you prefer.  
**index\_water** (in fortran or IDL)

They are both under <http://reef.atmos.colostate.edu/~odel1/at721/resources/codes/>

The index of refraction of water at visible to IR frequencies looks like this:



The index of refraction of water at microwave frequencies looks like this:

